

(3) 分母の有理化…分数の分母を根号のない形に直すこと。

㊂→「分母の $\sqrt{}$ 部分を分母・分子にかける」

$$\begin{aligned} \textcircled{1} \quad \sqrt{\frac{a}{b}} &= \frac{\sqrt{a} \times \sqrt{b}}{\sqrt{b} \times \sqrt{b}} \\ &= \frac{\sqrt{ab}}{b} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad \frac{a}{\sqrt{b}} &= \frac{a \times \sqrt{b}}{\sqrt{b} \times \sqrt{b}} \\ &= \frac{a\sqrt{b}}{b} \end{aligned}$$

(例1) 次の分数の分母を有理化しなさい。

$$\textcircled{1} \quad \frac{\sqrt{5}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$$

$$= \frac{\sqrt{10}}{2}$$

$$\textcircled{2} \quad \frac{9}{\sqrt{12}}$$

$$= \frac{9}{2\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$\textcircled{3} \quad \frac{4\sqrt{3}}{\sqrt{8}}$$

$$= \frac{2\sqrt{3}}{1} \times \frac{\sqrt{2}}{\sqrt{2}}$$

$$= \frac{3\sqrt{3}}{2}$$

$$= \frac{12\sqrt{6}}{2}$$

$$= \sqrt{6}$$

(4) 平方根の乗除II

$$\textcircled{1} \quad a\sqrt{b} \times c\sqrt{d} = ac\sqrt{bd}$$

$$\textcircled{2} \quad \frac{\sqrt{a}}{b} \times \frac{b\sqrt{b}}{a\sqrt{a}} = \frac{\sqrt{b}}{a}$$

(例2) 次の計算をしなさい。

$$\begin{aligned} \textcircled{1} \quad \sqrt{18} \times 3\sqrt{24} &= 3\sqrt{2} \times 6\sqrt{6} \\ &= 18\sqrt{12} \\ &= 36\sqrt{3} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad \frac{\sqrt{12}}{3} \div \frac{\sqrt{3}}{6} &= \frac{\cancel{\sqrt{12}}}{\cancel{3}} \times \frac{6}{\cancel{\sqrt{3}}} \\ &= 4 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad \sqrt{12} \div 6\sqrt{15} \times \sqrt{5} &= \frac{\cancel{\sqrt{12}} \times \cancel{\sqrt{5}}}{\cancel{6}\sqrt{\cancel{15}}} \\ &\leftarrow \sqrt{} \text{の約分} \\ &= \frac{1}{3} \quad \text{又有}\sqrt{} \text{がく！} \end{aligned}$$

☆

「の中は中どうし、「外は外どうしで

乗除、約分をする！

最後に分母の有理化と $a\sqrt{b}$ チェック！！

(5) 平方根の近似値

$$\boxed{\begin{array}{ll} \textcircled{1} \sqrt{100} = 10 & \textcircled{2} \sqrt{10000} = 100 \\ \textcircled{3} \sqrt{\frac{1}{100}} = \frac{1}{10} & \textcircled{4} \sqrt{\frac{1}{10000}} = \frac{1}{100} \end{array}}$$

(例3) $\sqrt{5} = 2.236$, $\sqrt{50} = 7.071$ として次の近似値を求めよ。

$$\textcircled{1} \sqrt{500} \quad \textcircled{2} \sqrt{500000} \quad \textcircled{3} \sqrt{0.50} \quad \textcircled{4} \sqrt{0.000050} \quad \textcircled{5} \sqrt{200}$$

$$\begin{aligned} &= \sqrt{5} \times \sqrt{100} & &= \sqrt{50} \times \sqrt{10000} & &= \sqrt{\frac{50}{100}} & &= \sqrt{\frac{50}{1000000}} & &= \sqrt{4} \times \sqrt{50} \\ &= 2.236 \times 10 & &= 7.071 \times 100 & &= \frac{\sqrt{50}}{\sqrt{100}} & &= \frac{\sqrt{50}}{\sqrt{1000000}} & &= 2 \times 7.071 \\ &= 22.36 & &= 707.1 & &= \frac{\sqrt{50}}{\sqrt{100}} & &= \frac{\sqrt{50}}{\sqrt{1000000}} & &= 14.142 \end{aligned}$$

$$\begin{aligned} &= 7.071 \times \frac{1}{10} & &= 7.071 \times \frac{1}{1000} & & \left(\begin{array}{l} 200 \div 5 = 40 \times \\ 200 \div 50 = 4 \text{ OK} \end{array} \right) \\ &= 0.7071 & &= 0.007071 & & \uparrow \end{aligned}$$

2乗の割合
1/5

(6) 平方根の加法・減法

(例4) 加法・減法…「」の中が同じものどうしは同類項としてまとめる！

$$\textcircled{1} \sqrt{50} - \sqrt{12} - \sqrt{8} + \sqrt{27}$$

$$= \underline{5\sqrt{2}} - \underline{2\sqrt{3}} - \underline{2\sqrt{2}} + \underline{3\sqrt{3}}$$

$$= \underline{\underline{3\sqrt{2}}} + \underline{\underline{\sqrt{3}}}$$

$$\textcircled{2} \sqrt{8} - \frac{3}{\sqrt{2}} \times \sqrt{2}$$

$$= 2\sqrt{2} - \frac{3\sqrt{2}}{2}$$

$$= \frac{4\sqrt{2}}{2} - \frac{3\sqrt{2}}{2}$$

$$= \frac{\sqrt{2}}{2}$$

通分